



Virtual University

About Us

MTH501  
Solved Final Term Paper 1

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Year  
2017

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بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

In the Name of Allāh, the Most Gracious, the Most Merciful

### Paper Pattern

MCQS 40 each 1 mark  
Short 4 each 2 marks  
Short 4 each 3 marks  
long 4 each 5 marks

Question No : 12 of 52

Marks: 1 (Budgeted Time 1 Min)

$\|u + v + w\| \leq \|u\| + \|v\| + \|w\|$  for all vectors  $u, v$  and  $w$  in an inner product space.

Answer ( Please select your correct option )

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True

☒

**correct**

False

☐

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Question No : 13 of 52

Marks: 1 (Budgeted Time 1 Min)

The dominant eigenvalue for the matrix  $A = \begin{bmatrix} 0 & 0 & 2 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & -3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$  is

Answer ( Please select your correct option )

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$\lambda = 1$

☐

$\lambda = -3$

☒

**correct**

$\lambda = -1$

☐

$\lambda = 0$

☐

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Question No : 14 of 52

Marks: 1 (Budgeted Time 1 Min)

A square matrix A is invertible if and only if  $x = 0$  is not an eigen value of A.

Answer ( Please select your correct option )

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True

☒

correct

False

☐

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Question No : 15 of 52

Marks: 1 (Budgeted Time 1 Min)

A square matrix with orthogonal columns \_\_\_\_\_ matrix. (Click on most appropriate)

Answer ( Please select your correct option )

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is an orthogonal

☒

correct

may be an orthogonal

☐

may not be an orthogonal

☐

is not an orthogonal

☐

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Question No : 16 of 52

Marks: 1 (Budgeted Time 1 Min)

If two rows are orthogonal, they are \_\_\_\_\_.

Answer ( Please select your correct option )

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linearly independent

☒

correct

linearly dependent

☐

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Question No : 17 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $x$  is orthogonal to both  $u$  and  $v$ , then  $x$  must be \_\_\_\_\_ to  $u + v$ .not sure

Answer ( Please select your correct option )

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☐ orthogonal☐ orthonormalcorrect☐ perpendicular☐ parallel

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Question No : 18 of 52

Marks: 1 (Budgeted Time 1 Min)

The given system  $\begin{matrix} 2x + 3y = 3 \\ 6x + 9y = 7 \end{matrix}$  has

Answer ( Please select your correct option )

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☐ Unique solution☐ Infinitely many solutions☐ No solutioncorrect☐ None of these

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Question No : 19 of 52

Marks: 1 (Budgeted Time 1 Min)

Which statement about the matrix  $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 7 & 2 & 0 & 0 \\ 9 & 1 & 2 & 0 \\ 5 & 4 & 2 & -1 \end{bmatrix}$  is false?

Answer ( Please select your correct option )

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☐ Eigenvalue 2 has Algebraic multiplicity 1☐ Eigenvalue of the matrix are 1, 2 and -1.☐ Characteristic polynomial of the matrix is  $(1 - \lambda)(2 - \lambda)^2(-1 - \lambda)$ .☐ Eigenvalue -1 has multiplicity 1.

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Question No : 20 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $A = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$  is diagonalizable then A has 2 distinct eigenvalues.

Answer ( Please select your correct option )

[WWW.VirtualAcademyLive.com](http://WWW.VirtualAcademyLive.com)☐ True☐☐ False☐**Made by: Waqar Siddhu**

Question No : 21 of 52

Marks: 1 (Budgeted Time 1 Min)

A is diagonalizable if  $A = PDP^{-1}$  Where

Answer ( Please select your correct option )

[WWW.VirtualAcademyLive.com](http://WWW.VirtualAcademyLive.com)☐ D is any matrix and P is an invertible matrix☐☐ D is a diagonal matrix and P is any matrix☐☐ D is a diagonal matrix and P is invertible matrix☐**correct**☐ D is a invertible matrix and P is any matrix☐**Made by: Waqar Siddhu**

Question No : 22 of 52

Marks: 1 (Budgeted Time 1 Min)

Which statement is FALSE.

Answer ( Please select your correct option )

[WWW.VirtualAcademyLive.com](http://WWW.VirtualAcademyLive.com)☐ If  $Ax = \lambda x$  for some real number  $\lambda$  then  $\lambda$  is known as eigenvalue of the matrix A.☐☐ The eigenvalues of any matrix are on its main diagonal.☐☐ In order to find the eigenvalues we solve the equation  $|A - \lambda I| = 0$ ☐☐ An eigenspaces of A is the Null space of some matrix.☐**correct****Made by: Waqar Siddhu**



Question No : 23 of 52

Marks: 1 (Budgeted Time 1 Min)

How many terms are there in the algebraic expression  $8x^2 + \sqrt{9x} \times 25x^3$ ?

Answer ( Please select your correct option )

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4

☐

3

☐

2

☐correct

1

☐

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Question No : 24 of 52

Marks: 1 (Budgeted Time 1 Min)

If two matrices are added, then which of the following should be true for them?

Answer ( Please select your correct option )

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Both must have same order.

☐correct

Both must have different order.

☐

Both must be rectangular.

☐

Both must be square.

☐

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Question No : 25 of 52

Marks: 1 (Budgeted Time 1 Min)

If a matrix  $A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 6 & 1 & 1 \end{bmatrix}$ , then which of the following is true for  $A$ ?

Answer ( Please select your correct option )

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It is a rectangular matrix.

☐

It is a row matrix.

☐

It is a singular matrix.

☐correct

It is a scalar matrix.

☐

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Question No : 26 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $\vec{v}_1, \vec{v}_2$  and  $\vec{v}_3$  are in  $R^m$  then which of the following is equivalent to  $[\vec{v}_1 \ \vec{v}_2 \ \vec{v}_3] \begin{bmatrix} 2 \\ -7 \\ 5 \end{bmatrix}$ ?

Answer ( Please select your correct option )

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☐  $2\vec{v}_1 - 7\vec{v}_2 + 5\vec{v}_3$ 
**correct**
☐  $5\vec{v}_1 - 7\vec{v}_2 + 2\vec{v}_3$ 
☐  $5\vec{v}_1 + 2\vec{v}_2 - 7\vec{v}_3$ 
☐  $2\vec{v}_1 + 5\vec{v}_2 - 7\vec{v}_3$ 
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Question No : 27 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $(\vec{v}_1, \vec{v}_2, \vec{v}_3)$  is linearly dependent set and  $\vec{v}_1 \neq c\vec{v}_2$  (where 'c' is a scalar), then which option is true?

Answer ( Please select your correct option )

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☐  $\vec{v}_1 \in \text{Span}\{\vec{v}_1, \vec{v}_2\}$ 
☐  $\vec{v}_2 \in \text{Span}\{\vec{v}_1, \vec{v}_2\}$ 
☐  $\vec{v}_3 \in \text{Span}\{\vec{v}_1, \vec{v}_2\}$ 
☐  $\vec{v}_3 \notin \text{Span}\{\vec{v}_1, \vec{v}_2\}$ 
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Question No : 28 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $A = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 0 & 1 \\ 0 & -1 & 1 \end{bmatrix}$ , then which of the following is true for the matrix A?

Answer ( Please select your correct option )

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☐ It is an invertible matrix.

☐ It is a singular matrix.

☐ It is a non-invertible matrix.
**correct**
☐ It is a rectangular matrix.
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Question No : 29 of 52

Marks: 1 (Budgeted Time 1 Min)

Which of the following is true for the partitioned matrices  $A = \begin{bmatrix} C & D \end{bmatrix}$  and  $B = \begin{bmatrix} E & F \end{bmatrix}$ , where sub-matrices  $C$  and  $D$  have the same sizes as  $E$  and  $F$  respectively ?

Answer ( Please select your correct option )

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☐  $A + B = \begin{bmatrix} CE & DF \end{bmatrix}$

☐  $A + B = \begin{bmatrix} C + E \\ D + F \end{bmatrix}$

☐  $A + B = \begin{bmatrix} C + E & D + F \end{bmatrix}$

☐  $A + B = \begin{bmatrix} CE \\ DF \end{bmatrix}$

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Question No : 30 of 52

Marks: 1 (Budgeted Time 1 Min)

If a matrix  $A$  is factorized into lower and upper triangular matrices, then which of the following is true for the matrix ?

Answer ( Please select your correct option )

[WWW.VirtualAcademyLive.com](http://WWW.VirtualAcademyLive.com)☐ It is called an  $LU$ -procedure.☐ It is called an  $LU$ -decomposition.☐ It is called an  $LU$ -matrices.☐ It is called an  $LU$ -algorithm.

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Question No : 31 of 52

Marks: 1 (Budgeted Time 1 Min)

If the matrix  $A = \begin{bmatrix} 1 & 5 & 4 \\ 0 & 1 & 7 \\ 0 & 0 & 0 \end{bmatrix}$ , then which of the following is true about it ?

Answer ( Please select your correct option )

[WWW.VirtualAcademyLive.com](http://WWW.VirtualAcademyLive.com)☐ Its determinant is 0.☐ Its determinant is 2.☐ Its determinant is 4.☐ Its determinant is 6.

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Question No : 32 of 52

Marks: 1 (Budgeted Time 1 Min)

Let a set  $S$  is a basis of a vector space  $V$ , then which of the following is NOT true about it ?

Answer ( Please select your correct option )

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☐ It is linearly dependent.

☐ Each element of  $S$  belongs to  $V$ .

☐ It spans  $V$ .

☐ It is linearly independent.

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Question No : 33 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $B = \left\{ \begin{pmatrix} 0 \\ 1 \end{pmatrix}, \begin{pmatrix} 2 \\ 0 \end{pmatrix} \right\}$  for  $\mathbb{R}^2$  and an  $\vec{x} \in \mathbb{R}^2$  has coordinate vector  $[\vec{x}]_B = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$ , then which of the following is the value of  $\vec{x}$  ?

Answer ( Please select your correct option )

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☐  $\vec{x} = \begin{pmatrix} 6 \\ 1 \end{pmatrix}$ 
☐  $\vec{x} = \begin{pmatrix} 2 \\ 0 \end{pmatrix}$ 
☐  $\vec{x} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ 
☐  $\vec{x} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$ 
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Question No : 34 of 52

Marks: 1 (Budgeted Time 1 Min)

If a set  $S = \{1, x, x^2\}$  is a basis for  $p_2$  and  $[\vec{p}]_S = (2, 4, 7)$ , then which of the following is the most appropriate option ?

Answer ( Please select your correct option )

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☐  $p_2 = 2 - 4x + 7x^2$ 
☐  $p_2 = 2 - 4x - 7x^2$ 
☐  $p_2 = 2 + 4x + 7x^2$ 
☐  $p_2 = 4x - 7x^2$ 
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Question No : 35 of 52

Marks: 1 (Budgeted Time 1 Min)

Which of the following is the set of standard basis for  $R^3$  ?

Answer ( Please select your correct option )

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☐  $\{(1, 1, 0), (0, 1, 0), (1, 0, 1)\}$

☐  $\{(1, 0, 0), (0, 1, 0), (0, 0, 1)\}$

☐  $\{(1, 0, 0), (1, 1, 0), (0, 0, 1)\}$

☐  $\{(1, 0, 0), (0, 1, 0), (1, 1, 1)\}$

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Question No : 36 of 52

Marks: 1 (Budgeted Time 1 Min)

Consider the bases for  $R^2$  given by  $B = \left\{ \begin{bmatrix} 1 \\ b_1 \end{bmatrix}, \begin{bmatrix} 1 \\ b_2 \end{bmatrix} \right\}$  and  $C = \left\{ \begin{bmatrix} c_1 \\ c_2 \end{bmatrix} \right\}$ ; where  $\begin{bmatrix} 1 \\ b_1 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ ,  $\begin{bmatrix} 1 \\ b_2 \end{bmatrix} = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$ ,  $\begin{bmatrix} c_1 \\ c_2 \end{bmatrix} = \begin{bmatrix} -5 \\ 3 \end{bmatrix}$ ,  $\begin{bmatrix} c_2 \\ c_1 \end{bmatrix} = \begin{bmatrix} -2 \\ 1 \end{bmatrix}$ , also assume that  $P_{B \leftarrow C} = \begin{bmatrix} -2 & -1 \\ 3 & 1 \end{bmatrix}$ ; then which of the following is the change-of-coordinates matrix from  $B$  to  $C$  ?

Answer ( Please select your correct option )

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☐  $P_{C \leftarrow B} = \begin{bmatrix} 1 & 1 \\ -3 & -2 \end{bmatrix}$

☐  $P_{C \leftarrow B} = \begin{bmatrix} 1 & -1 \\ 0 & 1 \end{bmatrix}$

☐  $P_{C \leftarrow B} = \begin{bmatrix} -5 & -2 \\ 3 & 1 \end{bmatrix}$

☐  $P_{C \leftarrow B} = \begin{bmatrix} -8 & -3 \\ 3 & 1 \end{bmatrix}$

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Question No : 37 of 52

Marks: 1 (Budgeted Time 1 Min)

If the general term of a typical signal is  $(0.6)^k$ , then determine which of the following is the signal for  $k = -2$  ?

Answer ( Please select your correct option )

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☐  $(0.6)^{-2} = 0$

☐  $(0.6)^{-2} = 0.6$

☐  $(0.6)^{-2} = (0.6)^2$

☐  $(0.6)^{-2} = 1/(0.6)^2$

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Question No : 38 of 52

Marks: 1 (Budgeted Time 1 Min)

If the Casorati matrix is not invertible, then which of the following is the most appropriate option regarding the associated signals?

Answer ( Please select your correct option )

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- ☐ The signals are linearly independent .
- ☐ The signals are linearly dependent .
- ☐ The signals may or may not dependent .
- ☐ The signals may or may not independent .

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Question No : 39 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $\{y_k\} = \{\dots, 1, 0.7, 0, -0.7, -1, -0.7, 0, 0.7, 1, 0.7, 0, \dots\}$  and  $0.35y_{k+2} + 0.6y_{k+1} + 0.42y_k = z_k$  ;  
 $\uparrow$   
 $k = 0$   
 then which of the following is the value of  $z_0$ ?

Answer ( Please select your correct option )

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- ☐ 0.840
- ☐ 0.049
- ☐ -0.770
- ☐ -1.139

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Question No : 39 of 52

Marks: 1 (Budgeted Time 1 Min)

If  $\{y_k\} = \{\dots, 1, 0.7, 0, -0.7, -1, -0.7, 0, 0.7, 1, 0.7, 0, \dots\}$  and  $0.35y_{k+2} + 0.6y_{k+1} + 0.42y_k = z_k$  ;  
 $\uparrow$   
 $k = 0$   
 then which of the following is the value of  $z_0$ ?

Answer ( Please select your correct option )

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- ☐ 0.840
- ☐ 0.049
- ☐ -0.770
- ☐ -1.139

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Question No : 40 of 52

Marks: 1 (Budgeted Time 1 Min)

Suppose that  $B = \{b_1, b_2\}$  is a basis for  $V$  and  $C = \{c_1, c_2, c_3\}$  is a basis for  $W$ . Let  $T: V \rightarrow W$  be a linear transformation with the property that  $T(b_1) = 5c_1 - 2c_2 + 3c_3$  and  $T(b_2) = 4c_1 - c_2 + 7c_3$ . Determine the value of  $[T(b_2)]_C$ ?

Answer ( Please select your correct option )

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☐  $\begin{bmatrix} 5 \\ -2 \\ 3 \end{bmatrix}$

☐  $\begin{bmatrix} 7 \\ -1 \\ 4 \end{bmatrix}$

☐  $\begin{bmatrix} 4 \\ -1 \\ 7 \end{bmatrix}$

☐  $\begin{bmatrix} 3 \\ -2 \\ 7 \end{bmatrix}$

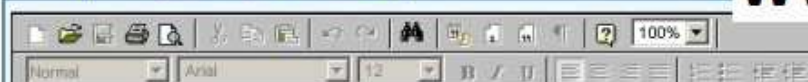
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Question No : 41 of 52

Marks: 2 (Budgeted Time 4 Min)

Determine whether the set of vectors are orthogonal or not.

$$\begin{bmatrix} 5 \\ -4 \\ 0 \\ 3 \end{bmatrix}, \begin{bmatrix} -4 \\ 1 \\ -3 \\ 8 \end{bmatrix}, \begin{bmatrix} 3 \\ 3 \\ 5 \\ 1 \end{bmatrix}$$

Answer ( Please [click here](#) to Add Answer )
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Question No : 41 of 52

Marks: 2 (Budgeted Time 4 Min)

$$\begin{bmatrix} 5 \\ -4 \\ 0 \\ 3 \end{bmatrix}, \begin{bmatrix} -4 \\ 1 \\ -3 \\ 8 \end{bmatrix}, \begin{bmatrix} 3 \\ 3 \\ 5 \\ 1 \end{bmatrix}$$

Answer ( Please [click here](#) to Add Answer )
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Question No : 42 of 52

Marks: 2 (Budgeted Time 4 Min)

Is the following set of vectors is orthogonal with respect to the Euclidean inner product on  $\mathbb{R}^3$ ?

$$\left( \frac{1}{\sqrt{6}}, \frac{1}{\sqrt{6}}, -\frac{2}{\sqrt{6}} \right), \left( \frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0 \right)$$

Answer ( Please [click here](#) to Add Answer )

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Question No : 43 of 52

Marks: 2 (Budgeted Time 4 Min)

If a matrix  $A = \begin{bmatrix} 1 & 4 & 5 \\ 4 & 5 & 6 \\ 7 & 8 & 8 \end{bmatrix}$  and  $\det(A^t) = 6$ , then find the determinant of the matrix.

Answer ( Please [click here](#) to Add Answer )

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Question No : 44 of 52

Marks: 2 (Budgeted Time 4 Min)

Let  $B = \{b_1, b_2, b_3\}$  and  $D = \{d_1, d_2\}$  be bases for vector spaces  $V$  and  $W$ , respectively. Let  $T: V \rightarrow W$  be a linear transformation with the property that  $T(b_1) = 3d_1 - 5d_2$ ,  $T(b_2) = -d_1 + 6d_2$  and  $T(b_3) = 4d_2$ . Find a matrix  $M$  for  $T$  relative to  $B$  and  $D$ .

Answer ( Please [click here](#) to Add Answer )

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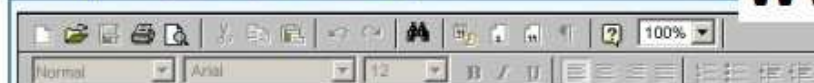
Question No : 45 of 52

Marks: 3 (Budgeted Time 6 Min)

Determine whether the vectors  $y = \begin{bmatrix} -3 \\ 7 \\ 4 \\ 0 \end{bmatrix}$ ,  $z = \begin{bmatrix} 1 \\ -8 \\ 15 \\ -7 \end{bmatrix}$  are orthogonal

Answer ( Please [click here](#) to Add Answer )

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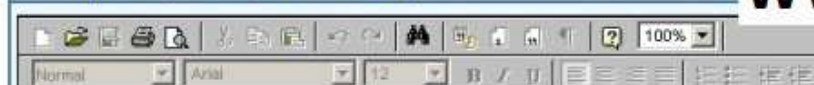
Question No : 46 of 52

Marks: 3 (Budgeted Time 6 Min)

Let  $W = \text{Span} (x_1, x_2)$ , where  $x_1 = \begin{bmatrix} 3 \\ 0 \\ -1 \end{bmatrix}$ ,  $x_2 = \begin{bmatrix} 8 \\ 5 \\ -6 \end{bmatrix}$ . Construct an orthogonal basis  $(v_1, v_2)$  for  $W$ .

Answer ( Please [click here](#) to Add Answer )

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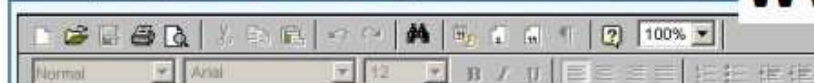
Question No : 47 of 52

Marks: 3 (Budgeted Time 6 Min)

If  $A = \begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix}$  then find an invertible matrix  $P$  such that  $P^{-1}AP = D$  (diagonal matrix)

Answer ( Please [click here](#) to Add Answer )

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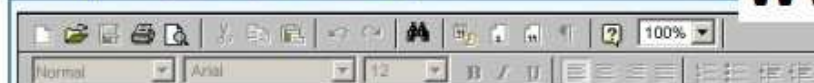
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Marks: 3 (Budgeted Time 6 Min)

Let  $\vec{v}_1 = \begin{bmatrix} 1 \\ 0 \\ -2 \end{bmatrix}$ ,  $\vec{v}_2 = \begin{bmatrix} -2 \\ 1 \\ 7 \end{bmatrix}$  and  $\vec{y} = \begin{bmatrix} h \\ -3 \\ -5 \end{bmatrix}$ . For what value(s) of 'h' is  $\vec{y}$  in the plane generated by  $\vec{v}_1$  and  $\vec{v}_2$ ?

Answer ( Please [click here](#) to Add Answer )

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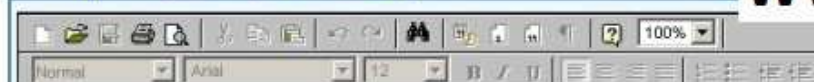
Question No : 49 of 52

Marks: 5 (Budgeted Time 10 Min)

Compute the least square error associated with the least square solution  $\hat{x} = \begin{bmatrix} 4 \\ 3 \\ -1 \\ 3 \end{bmatrix}$  of the equation  $Ax = b$  where  $A = \begin{bmatrix} 1 & -2 \\ -1 & 2 \\ 0 & 3 \\ 2 & 5 \end{bmatrix}$ ,  $b = \begin{bmatrix} 3 \\ 1 \\ -4 \\ 2 \end{bmatrix}$

Answer ( Please [click here](#) to Add Answer )

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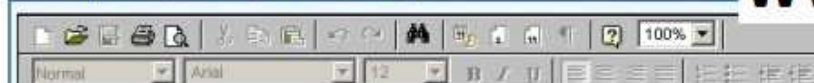
Marks: 5 (Budgeted Time 10 Min)

Find the dominant Eigen pair (i.e. the Eigen value and Eigen vector) by using the Power Method for the following matrix. (Perform only 1 iteration)

$$A = \begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}, \quad x_0 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

Answer ( Please [click here](#) to Add Answer )

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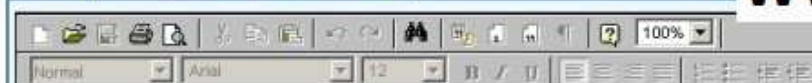
Question No : 51 of 52

Marks: 5 (Budgeted Time 10 Min)

Find  $A^2$ , given that  $A = PDP^{-1}$ , where P and D are given below  $A = \begin{pmatrix} 2 & 6 \\ -4 & 12 \end{pmatrix}$ ,  $P = \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix}$ ,  $D = \begin{pmatrix} 6 & 0 \\ 0 & 8 \end{pmatrix}$ ,  $P^{-1} = \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix}$

Answer ( Please [click here](#) to Add Answer )

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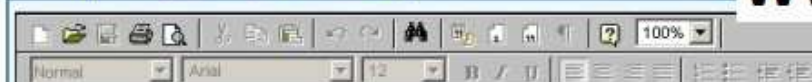
Question No : 52 of 52

Marks: 5 (Budgeted Time 10 Min)

Let  $A = \begin{bmatrix} 1 & 4 \\ 5 & 6 \end{bmatrix}$  and  $\vec{c} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$ . Define  $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  by  $T(\vec{x}) = A\vec{x}$ . Determine if  $\vec{c}$  is in the range of the transformation  $T$ .

Answer ( Please [click here](#) to Add Answer )

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Question No : 1 of 52

Marks: 1 (Budgeted Time 1 Min)

Which statement about the General Least Square Method is true?

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Answer ( Please select your correct option )

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☐

Solution obtained by this method is always unique.

☐

This is a numerical method for the solution of System of Linear Equations.

☒This method find an  $x$  that makes  $Ax$  as close as possible to the  $b$ .correct☐

This method gives us exact solution of the system.

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Question No : 2 of 52

Marks: 1 (Budgeted Time 1 Min)

Let  $v = (1, -2, 2, 0)$ . The unit vector in the same direction as  $v$  is

Answer ( Please select your correct option )

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☐  $\left(\frac{1}{3}, \frac{2}{3}, \frac{2}{3}, 0\right)$

☐  $\left(\frac{1}{3}, -\frac{2}{3}, \frac{2}{3}, 0\right)$

☐  $\left(\frac{-1}{3}, \frac{2}{3}, \frac{-2}{3}, 0\right)$

☐  $\left(\frac{1}{3}, -\frac{2}{3}, \frac{2}{3}, \frac{1}{3}\right)$

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Question No : 3 of 52

Marks: 1 (Budgeted Time 1 Min)

Let  $u = (3, -2)$ ,  $v = (4, 5)$ . For the weighted Euclidean inner product  $\langle u, v \rangle = 4u_1v_1 + 5u_2v_2$   
 $\langle v, u \rangle =$

Answer ( Please select your correct option )

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☐ 2

☐ -2

☐ 3

☐ -3

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Question No : 4 of 52

Marks: 1 (Budgeted Time 1 Min)

Let  $v = (0, 2, 2, 1)$ . The unit vector in the same direction as  $v$  is

Answer ( Please select your correct option )

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☐  $\left(0, \frac{2}{3}, \frac{2}{3}, \frac{-1}{3}\right)$

☐  $\left(0, -\frac{2}{3}, \frac{2}{3}, \frac{-1}{3}\right)$

☐  $\left(0, \frac{2}{3}, \frac{2}{3}, \frac{1}{3}\right)$

☐  $\left(0, -\frac{2}{3}, \frac{2}{3}, \frac{1}{3}\right)$

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Question No : 5 of 52

Marks: 1 (Budgeted Time 1 Min)

Let  $\mathbb{R}^3$  have the Euclidean inner product. Then  $u = (2, 1, 3), v = (1, 7, k)$  are orthogonal for

Answer ( Please select your correct option )

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☐  $k = 9$

☐  $k = -3$

☐  $k = -9$

☐  $k = 3$

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Question No : 6 of 52

Marks: 1 (Budgeted Time 1 Min)

Let  $A$  be  $n \times n$  matrix whose entries are real. If  $\lambda$  is an eigenvalue of  $A$  with  $x$  a corresponding eigenvector in  $\mathbb{R}^n$ , then

Answer ( Please select your correct option )

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☐  $A\bar{x} = \lambda\bar{x}$

☐  $A\bar{x} = \overline{\lambda x}$

☐  $A\bar{x} = \overline{\lambda}x$

☐  $A\bar{x} = \lambda^{-1}\bar{x}$

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Question No : 7 of 52

Marks: 1 (Budgeted Time 1 Min)

Suppose that  $A = \begin{bmatrix} 1.25 & -.75 \\ -.75 & 1.25 \end{bmatrix}$  has eigenvalues 2 and 0.5. Then origin is a

origin 'O' is called the saddle point because one eigenvalue is greater than 1 in magnitude and one is less than 1 in magnitude.

Answer ( Please select your correct option )

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☐ Saddle pointcorrect☐ Repellor☐ Attractor

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Question No : 8 of 52

Marks: 1 (Budgeted Time 1 Min)

Suppose that  $A = \begin{bmatrix} 0.5 & 0.6 \\ -0.3 & 1.4 \end{bmatrix}$  has eigenvalues 0.8 and 1.1. Then origin is a

Answer ( Please select your correct option )

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☐ Saddle point**correct**☐ Repellor☐ Attractor**Made by: Waqar Siddhu**

Question No : 9 of 52

Marks: 1 (Budgeted Time 1 Min)

If A is an  $m \times n$  matrix with linearly independent column vectors, then A can be factored as  
 $A = QR$   
Where Q is an  $m \times n$  matrix with orthonormal column vectors, and R is an  $n \times n$

Answer ( Please select your correct option )

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☐ Upper triangular matrix☐ Invertible matrix☐ Invertible lower triangular matrix☐ Invertible upper triangular matrix**Made by: Waqar Siddhu**

Question No : 10 of 52

Marks: 1 (Budgeted Time 1 Min)

The matrix equation  $A^T A \hat{x} = A^T b$  represents a system of linear equations commonly referred to as the

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Answer ( Please select your correct option )

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☐ normal equations for  $x$ ☐ normal equations for  $\hat{x}$ **correct**☐ normal equations for  $A$ ☐ normal equations for  $b$ **Made by: Waqar Siddhu**



By the Best Approximation Theorem, the distance from  $y$  to  $W$  is  $\|y - \hat{y}\|$ , where  $\hat{y} =$

Answer ( Please select your correct option )

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☐  $\text{proj}_W \hat{y}$

☐  $\text{proj}_W y$

correct

☐  $\text{proj}_y W$

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